

## COMET V.5.0 – BM V.1.0

### CASE BMNL-2A: PLANE STRAIN RIGID PUNCH (PERFECT PLASTICITY MATERIAL)

ISSUE: 1 (Publication date: 12/04/2013)

#### Summary

##### Model:

- Rigid, frictionless punch is pressed into a deep plate of finite width supported on a frictionless plane.
- 2D plane strain conditions
- Controlled loading.
- Perfect plasticity material.

##### References:

Linkens, D., *Selected Benchmarks for Material Non-Linearity*, Published by NAFEMS  
Committed to Professional Development for Engineering Analysis & Simulation, Ref: R0026,  
p.20,URL: [http://www.nafems.org/publications/browse\\_buy/nonlinear/r0026/](http://www.nafems.org/publications/browse_buy/nonlinear/r0026/)

##### Element type(s) tested

Description	Designation	COMET model	See in DATA INPUT MANUAL V.5.0
Linear triangular 2D element - 3 nodes	L-TRIANG3-R	BMNL-2A-rigid-punch-and-plate-perfplast-L-triaR.gid	Secc. 4, pp. 41, 61
Parabolic triangular 2D element – 6 nodes	Q-TRIANG6-R	BMNL-2A-rigid-punch-and-plate-perfplast-Q-triaR.gid	Secc. 4, pp. 41, 61
Linear Quadrilateral 2D element – 4 nodes	L-QUADR4-R	BMNL-2A-rigid-punch-and-plate-perfplast-L-quadR.gid	Secc. 4, pp. 42, 61
Parabolic quadrilateral 2D element – 8 nodes (Not included in this issue)	Q-QUADR8	Not included	Secc. 4, pp. 42, 61



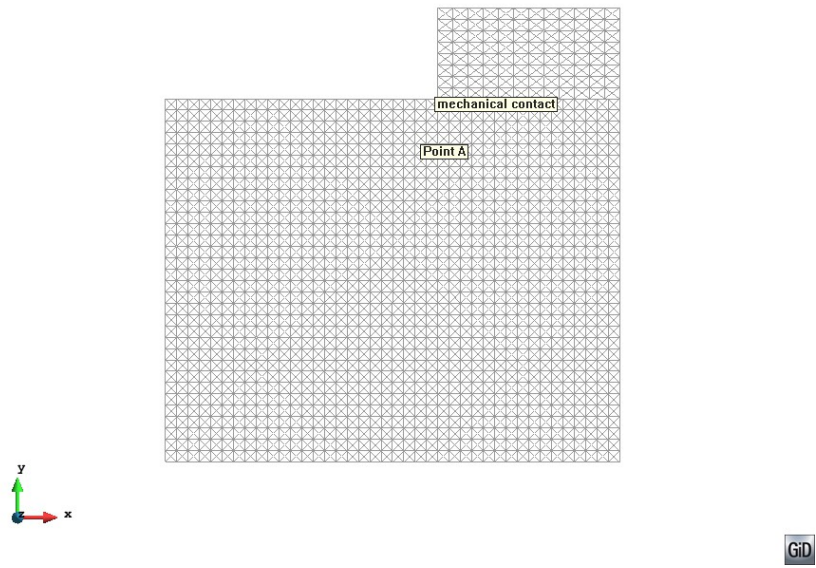


Figure 3: High rigid punch and deep plate, contact and test point definitions over 32x40x4 L-TRIANG3-R finite elements mesh.

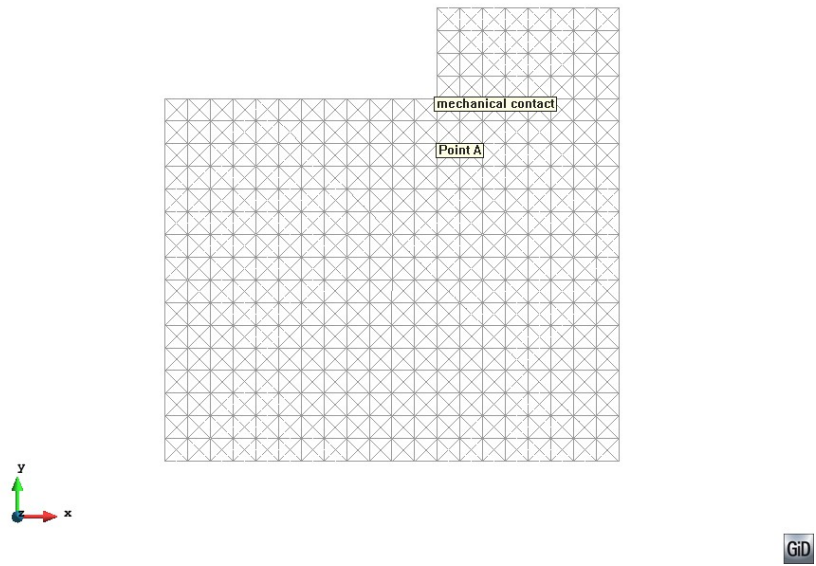


Figure 4: High rigid punch and deep plate, contact and test point definitions over 16x20x4 Q-TRIANG6-R finite elements mesh.

Data related to the test case can be shown in Table2

Material Properties	Geometric and mesh properties	Loading
<p><b>Punch:</b>  <math>E=1000000</math>  <math>\nu = 0,3</math>  Elastic model</p> <p><b>Deep plate:</b>  <math>E = 1000</math>  <math>\nu = 0,3</math>  Yield stress= 1.0  Von Mises yield, associated flow rule  H: 0 (Perfect plasticity)</p>	<p><b>Geometry dimensions:</b> See fig. 1</p> <p><b>Meshes characteristics:</b>  For L-QUADR4-R elems.:  Punch mesh: 8x16  Plate mesh: 32x40</p> <p>For L-TRIANG3-R elems.:  Punch mesh: 16x32  Plate mesh: 32x40x4 (each Quadrilateral element is divided en 4 triangles).</p> <p>For Q-TRIANG6-R elems.:  Punch mesh: 4x8  Plate mesh: 16x20x4 (each Quadrilateral element is divided en 4 triangles).</p>	$P_0 = 108.8$ (applied on superior punch surface).

Table 2: Analysis data

## Analysis

Symmetry properties of the geometry (**iError! No se encuentra el origen de la referencia.1**, represent the result over the whole plate only with 2D elements mesh (Figure ). Plane strain conditions are assumed.

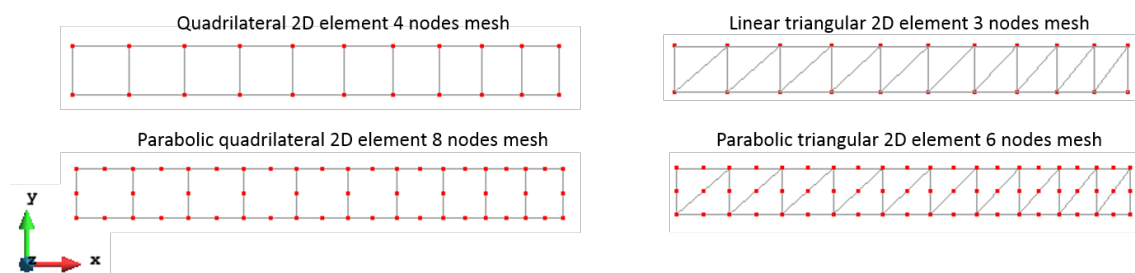


Figure 4: 2D test case mesh and elements type tested (Q-QUADR8 elem. is not tested at this issue)

## Results analysis

Dimension	Element type	Reference solution	COMET result	Relative error
2D (Plane strain)	Linear triangular 2D element (at A point for P=108.8 and Deflection of punch=0.18)	$\sigma_{xx} = -0.203$ $\sigma_{yy} = -0.944$ $\sigma_{xy} = -0.441$	$\sigma_{xx} = 0.202$ $\sigma_{yy} = 0.891$ $\sigma_{xy} = 0.457$	0.1% 5.6% 3.8%
	Parabolic triangular 2D element (at A point for P=108.8 and deflection of punch=0.18)	$\sigma_{xx} = -0.203$ $\sigma_{yy} = -0.944$ $\sigma_{xy} = -0.441$	$\sigma_{xx} = 0.199$ $\sigma_{yy} = 0.963$ $\sigma_{xy} = 0.412$	1.97% 2.01% 6.6%
	Linear Quadrilateral 2D element (at A point for P=108.8 and deflection of punch = 0.18)	$\sigma_{xx} = -0.203$ $\sigma_{yy} = -0.944$ $\sigma_{xy} = -0.44$	$\sigma_{xx} = -0.187$ $\sigma_{yy} = -0.917$ $\sigma_{xy} = -0.446$	7.9 % 2.8 % 1.36 %

Table 3: Results analysis summary

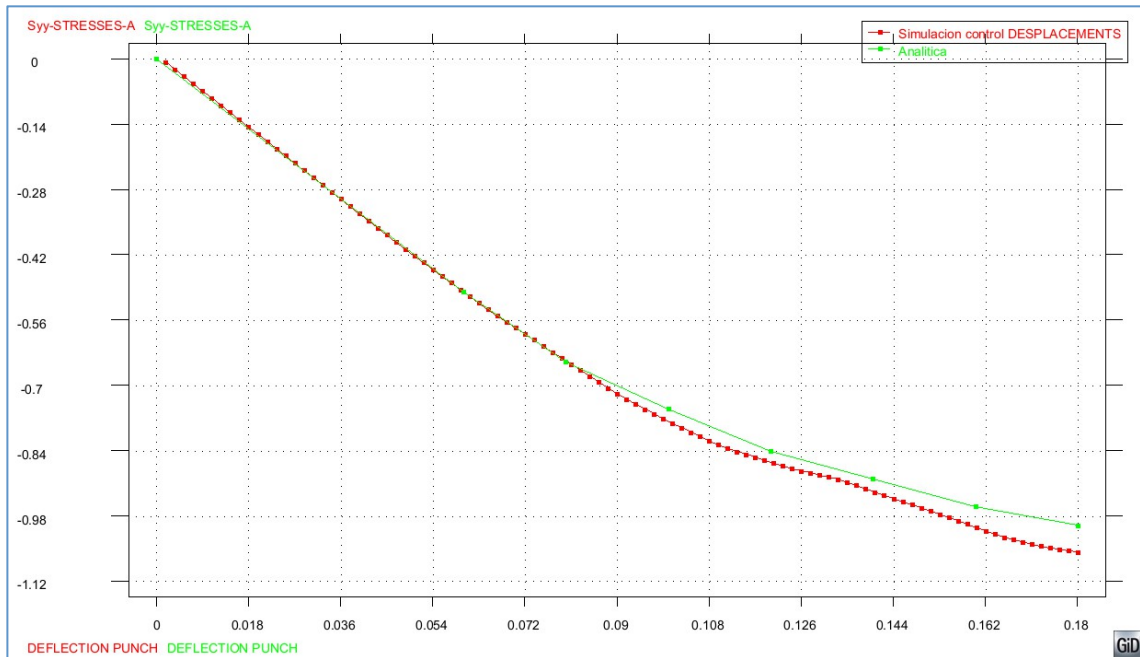


Figure 5 : Applied deflection of Punch evrsus STRESSYY at point A with control DISPLACEMENTS